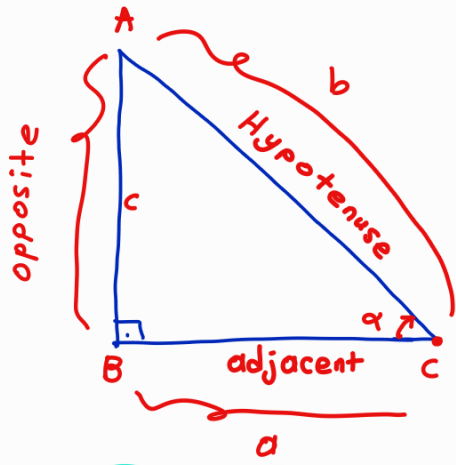


= Trigonometry Formulas =



$$\sin \alpha = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{c}{b}$$

$$\cos \alpha = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{a}{b}$$

$$\tan \alpha = \frac{\text{opposite}}{\text{adjacent}} = \frac{c}{a}$$

$$\cot \alpha = \frac{\text{adjacent}}{\text{opposite}} = \frac{a}{c}$$

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\cot \alpha = \frac{\cos \alpha}{\sin \alpha}$$

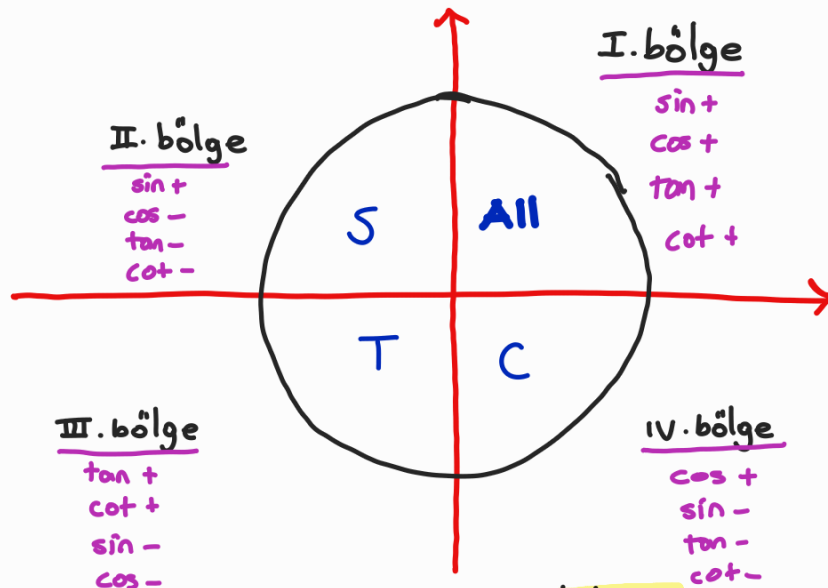
$$\Rightarrow \sec \alpha = \frac{1}{\cos \alpha}$$

$$\Rightarrow \operatorname{cosec} \alpha = \frac{1}{\sin \alpha}$$

$$\star \tan x \cdot \cot x = 1$$

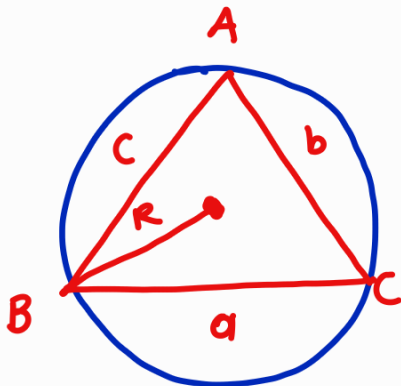
$$\sin^2 \alpha + \cos^2 \alpha = 1 \quad \star \text{important!}$$

Signs of Trigonometric Functions



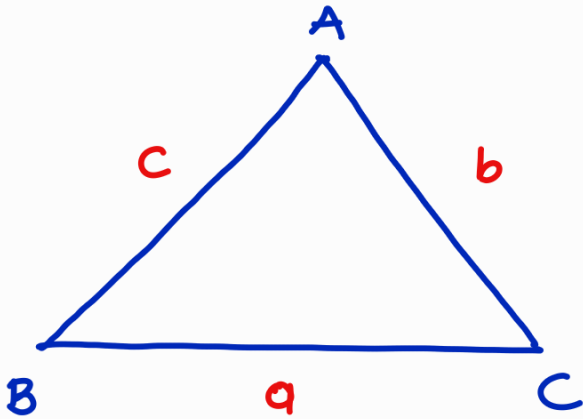
www.sorumatik.co

The Law of Sines



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = 2R$$

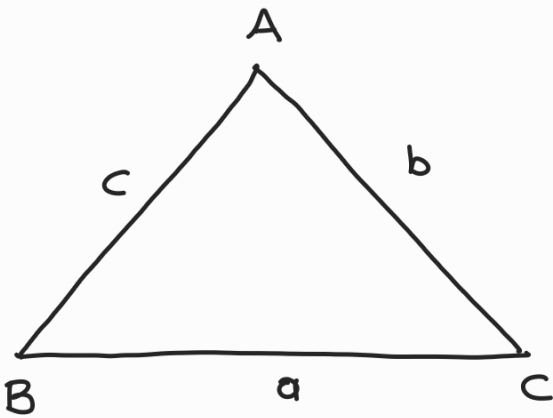
Sine area Formula



$$\begin{aligned}A(ABC) &= \frac{1}{2} \cdot b \cdot c \cdot \sin \hat{A} \\ &= \frac{1}{2} \cdot a \cdot b \cdot \sin \hat{C} \\ &= \frac{1}{2} \cdot a \cdot c \cdot \sin \hat{B}\end{aligned}$$

Sorumatik.co

The Law of Cosines



$$a^2 = b^2 + c^2 - 2bc \cdot \cos \hat{A}$$

$$b^2 = a^2 + c^2 - 2ac \cdot \cos \hat{B}$$

$$c^2 = a^2 + b^2 - 2ab \cdot \cos \hat{C}$$

Formulas sum and Difference identities:

- $\sin(a+b) = \sin a \cdot \cos b + \sin b \cdot \cos a$
- $\sin(a-b) = \sin a \cdot \cos b - \sin b \cdot \cos a$
- $\cos(a+b) = \cos a \cdot \cos b - \sin a \cdot \sin b$
- $\cos(a-b) = \cos a \cdot \cos b + \sin a \cdot \sin b$
- $\tan(a+b) = \frac{\tan a + \tan b}{1 - \tan a \cdot \tan b}$
- $\tan(a-b) = \frac{\tan a - \tan b}{1 + \tan a \cdot \tan b}$
- $\cot(a+b) = \frac{\cot a \cdot \cot b - 1}{\cot a + \cot b}$
- $\cot(a-b) = \frac{\cot a \cdot \cot b - 1}{\cot a - \cot b}$

Formulas Involving Double Angle Identities:

$$\bullet \sin 2a = 2 \cdot \sin a \cdot \cos a$$

$$\bullet \tan 2a = \frac{2 \tan a}{1 - \tan^2 a}$$

$$\begin{aligned} \bullet \cos 2a &= \cos^2 a - \sin^2 a \\ &= 2 \cos^2 a - 1 \\ &= 1 - 2 \sin^2 a \end{aligned}$$

$$\bullet \cot 2a = \frac{\cot^2 a - 1}{2 \cot a}$$

Formulas Involving Sum to Product Identities:

$$\bullet \sin a + \sin b = 2 \sin \left(\frac{a+b}{2} \right) \cdot \cos \left(\frac{a-b}{2} \right)$$

$$\bullet \sin a - \sin b = 2 \cdot \sin \left(\frac{a-b}{2} \right) \cdot \cos \left(\frac{a+b}{2} \right)$$

$$\bullet \cos a + \cos b = 2 \cos \left(\frac{a+b}{2} \right) \cdot \cos \left(\frac{a-b}{2} \right)$$

$$\bullet \cos a - \cos b = 2 \sin \left(\frac{a+b}{2} \right) \cdot \sin \left(\frac{a-b}{2} \right)$$

$$\bullet \tan a + \tan b = \frac{\sin(a+b)}{\cos a \cdot \cos b}$$

$$\bullet \tan a - \tan b = \frac{\sin(a-b)}{\cos a \cdot \cos b}$$

sorumatik.co

Formulas Involving Product Identities:

$$\bullet \sin a \cdot \cos b = \frac{1}{2} [\sin(a+b) + \sin(a-b)]$$

$$\bullet \cos a \cdot \cos b = \frac{1}{2} [\cos(a+b) + \cos(a-b)]$$

$$\bullet \sin a \cdot \sin b = -\frac{1}{2} [\cos(a+b) - \cos(a-b)]$$

Trigonometric Ratio Table:

Trigonometric Table

Degree	0°	30°	45°	60°	90°	180°	270°	360°
Radian	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	π	$\frac{3\pi}{2}$	2π
sin	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1	0	-1	0
cos	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	-1	0	1
tan	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	Not defined	0	Not defined	0
cosec	Not defined	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1	Not defined	-1	Not defined
sec	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	Not defined	-1	Not defined	1
cot	Not defined	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0	Not defined	0	Not defined

Single and double function:

$$\sin(-x) = -\sin x$$

$$\tan(-x) = -\tan x$$

$$\cot(-x) = -\cot x$$

} single
func.

$$\cos(-x) = \cos x$$

↓
double func.

